

Haskell4Life: Introduction

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Slides and code examples available online:

`http://lacl.fr/~sivanov/doku.php?id=en:
haskell_for_life`

Overlaps Between Programming and Cooking

<https://wiki.haskell.org/wikiupload/8/86/HaskellBCurry.jpg>

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1. Cooking receipt = program

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Haskell B. Curry

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Overlaps Between Programming and Cooking

1. Cooking receipt = program

2.



Haskell B. Curry



(joke)

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Outline

1. The Basics
2. The Types
3. The Functions
4. The Real Functional Programming
5. The Fun

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5. The Fun

Getting Started

- ▶ **Install** Haskell: `https://www.haskell.org/platform/`
- ▶ **Run** interactively: `ghci`
- ▶ **Compile**: `ghc source.hs -o executable`
- ▶ Get all kinds of **help**: `https://www.haskell.org/`

Getting Started

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There are Haskell syntax highlighting modules in all major IDEs and Haskell modes in Emacs and Vim.

Saying Hello

```
λ> putStrLn "Hello World!"
```

```
Hello World
```

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- ▶ call the function `putStrLn` with with **one argument**

Saying Hello

```
λ> putStrLn "Hello World!"
```

```
Hello World
```

- ▶ call the function `putStrLn` with with **one argument**
- ▶ **no** parentheses
- ▶ **no** commas
- ▶ **no** semicolons

Haskell Calculator

```
λ> 1 + 2
```

Haskell Calculator

```
λ> 1 + 2  
3
```

Haskell Calculator

```
λ> 1 + 2  
3
```

```
λ> 2 * 3
```


Haskell Calculator

$\lambda >$ 1 + 2

3

$\lambda >$ 2 * 3

6

Haskell Calculator

```
λ> 1 + 2  
3
```

```
λ> 2 * 3  
6
```

```
λ> (+) 1 2
```

Haskell Calculator

```
λ> 1 + 2  
3
```

```
λ> 2 * 3  
6
```

```
λ> (+) 1 2  
3
```

Haskell Calculator

```
λ> 1 + 2
```

```
3
```

```
λ> 2 * 3
```

```
6
```

```
λ> (+) 1 2
```

```
3
```

(+) is a **function** of two arguments.

Haskell Calculator

```
λ> 1 + 2
```

```
3
```

```
λ> 2 * 3
```

```
6
```

```
λ> (+) 1 2
```

```
3
```

(+) is a **function** of two arguments.

Normal functions are usually written in **prefix** form.

- ▶ `putStrLn "Hello"`

Haskell Calculator

```
λ> 1 + 2
```

```
3
```

```
λ> 2 * 3
```

```
6
```

```
λ> (+) 1 2
```

```
3
```

(+) is a **function** of two arguments.

Normal functions are usually written in **prefix** form.

- ▶ `putStrLn "Hello"`

Operators are usually written in **infix** form.

- ▶ `1 + 2`

Haskell Calculator

```
λ> 1 + 2  
3
```

```
λ> 2 * 3  
6
```

```
λ> (+) 1 2  
3
```

(+) is a **function** of two arguments.

Normal functions are usually written in **prefix** form.

- ▶ `putStrLn "Hello"`

Operators are usually written in **infix** form.

- ▶ `1 + 2`

Parentheses are used to write **operators** in **prefix** form.

- ▶ `(+) 1 2`

Negative Numbers

```
λ> 2 + -3
```


Negative Numbers

```
λ> 2 + -3
```

```
<interactive>:12:1-6:
```

```
  Precedence parsing error
```

```
    cannot mix '+' [infixl 6] and prefix '-' [infixl 6]  
    in the same infix expression
```

Negative Numbers

```
λ> 2 + -3
```

```
<interactive>:12:1-6:
```

```
  Precedence parsing error
```

```
    cannot mix '+' [infixl 6] and prefix '-' [infixl 6]  
    in the same infix expression
```

Parsing ambiguity!

How does one parse `function - 3`:

- ▶ apply `function` to `-3`?
- ▶ subtract `3` from `function`?

Negative Numbers

```
λ> 2 + -3
```

```
<interactive>:12:1-6:
```

```
  Precedence parsing error
```

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    cannot mix '+' [infixl 6] and prefix '-' [infixl 6]  
    in the same infix expression
```

Parsing ambiguity!

How does one parse `function - 3`:

- ▶ apply `function` to `-3`?
- ▶ subtract `3` from `function`?

```
λ> 2 + (-3)
```

```
-1
```

Boolean Values and Operators

```
λ> True && False
```

```
False
```

```
λ> True || False
```

```
True
```

Boolean Values and Operators

```
λ> True && False
```

```
False
```

```
λ> True || False
```

```
True
```

No direct coercion to/from numbers:

```
λ> True && 1
```

... won't work :-)

Comparison Operators

Typical comparison operators:

```
λ> 1 == 2
```

```
False
```

```
λ> 1 <= 2
```

```
True
```

Comparison Operators

Typical comparison operators:

```
λ> 1 == 2
```

```
False
```

```
λ> 1 <= 2
```

```
True
```

Unusual “not equals”:

```
λ> 1 /= 2
```

```
True
```

Variables

```
λ> let a = 1
```


Variables

```
λ> let a = 1
```

```
λ> a
```

```
1
```

Variables

```
λ> let a = 1
```

```
λ> a
```

```
1
```

```
λ> a + 1
```

```
2
```

Variables

```
λ> let a = 1
```

```
λ> a
```

```
1
```

```
λ> a + 1
```

```
2
```

```
λ> let e = exp 1
```

```
λ> e
```

```
2.718281828459045
```

Lists

```
λ> [1,2,3]
```

```
[1,2,3]
```

Lists

```
λ> [1,2,3]
```

```
[1,2,3]
```

```
λ> [1..5]
```

```
[1,2,3,4,5]
```

Lists

```
λ> [1,2,3]
```

```
[1,2,3]
```

```
λ> [1..5]
```

```
[1,2,3,4,5]
```

```
λ> [True, "three"]
```

```
... type error
```

Lists

```
λ> [1,2,3]
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```
[1,2,3]
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```
λ> [1..5]
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```
[1,2,3,4,5]
```

```
λ> [True, "three"]
```

```
... type error
```

All elements of a list must be of the same type.

Lists

```
λ> [1,2,3]
```

```
[1,2,3]
```

```
λ> 1:[2,3]
```

```
[1,2,3]
```

```
λ> [1..5]
```

```
[1,2,3,4,5]
```

```
λ> [True, "three"]
```

... type error

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Lists

```
λ> [1,2,3]
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```
[1,2,3]
```

```
λ> [1..5]
```

```
[1,2,3,4,5]
```

```
λ> [True, "three"]
```

... type error

```
λ> 1:[2,3]
```

```
[1,2,3]
```

```
λ> [1,2,3] ++ [4,5]
```

```
[1,2,3,4,5]
```

All elements of a list must be of the same type.

Lists

```
λ> [1,2,3]
```

```
[1,2,3]
```

```
λ> [1..5]
```

```
[1,2,3,4,5]
```

```
λ> [True, "three"]
```

```
... type error
```

```
λ> 1:[2,3]
```

```
[1,2,3]
```

```
λ> [1,2,3] ++ [4,5]
```

```
[1,2,3,4,5]
```

```
λ> length [4,5]
```

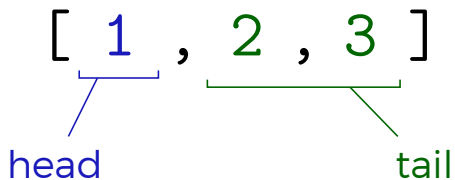
```
2
```

All elements of a list must be of the same type.

Lists: Heads and Tails

```
[ 1 , 2 , 3 ]
```

Lists: Heads and Tails



Lists: Heads and Tails

```
let xs = [ 1, 2, 3 ]
```

The diagram illustrates the decomposition of a list into its head and tail. In the list `[1, 2, 3]`, the element `1` is the head, and the list `[2, 3]` is the tail. The head is highlighted with a blue bracket and labeled 'head', while the tail is highlighted with a green bracket and labeled 'tail'.

Lists: Heads and Tails

```
let xs = [ 1 , 2 , 3 ]
```

Diagram illustrating the decomposition of the list `xs = [1 , 2 , 3]`. The element `1` is identified as the `head` (indicated by a blue bracket and label). The elements `2` and `3` are identified as the `tail` (indicated by a green bracket and label).

```
λ> head xs  
1
```

```
λ> tail xs  
[2,3]
```

Lists: Heads and Tails

```
let xs = [ 1 , 2 , 3 ]
```

Diagram illustrating the decomposition of the list `xs` into its head and tail. The head is the first element, `1`, and the tail is the remaining elements, `[2, 3]`.

```
λ> head xs  
1
```

```
λ> tail xs  
[2,3]
```

```
∀ list. list == (head list) : (tail list)  
[1,2,3] == 1 : [2,3]
```

Strings as Lists

```
λ> putStrLn "String"  
String
```


Strings as Lists

```
λ> putStrLn "String"
```

```
String
```

```
λ> "String" == ['S','t','r','i','n','g']
```

```
True
```

Strings as Lists

```
λ> putStrLn "String"
```

```
String
```

```
λ> "String" == ['S','t','r','i','n','g']
```

```
True
```

```
λ> "" == []
```

```
True
```

Strings as Lists

```
λ> putStrLn "String"
```

```
String
```

```
λ> "String" == ['S','t','r','i','n','g']
```

```
True
```

```
λ> "" == []
```

```
True
```

```
λ> 'a':"bc"
```

```
abc
```

Tuples

```
λ> (1,2,3)
```

```
(1,2,3)
```

```
λ> (True, "three")
```

```
(True, "three")
```

Tuples can contain values of **different types**.

Tuples

```
λ> (1,2,3)
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Tuples can contain values of **different types**.

Tuples are very **“strict”**: **no** concatenation, **no** indexing.

Tuples

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Tuples can contain values of **different types**.

Tuples are very **“strict”**: **no** concatenation, **no** indexing.

```
λ> fst (1,2)
```

```
1
```

```
λ> fst (1,2,3)
```

```
... type error
```

Tuples

```
λ> (1,2,3)
```

```
(1,2,3)
```

```
λ> (True, "three")
```

```
(True, "three")
```

Tuples can contain values of **different types**.

Tuples are very “**strict**”: **no** concatenation, **no** indexing.

```
λ> fst (1,2)
```

```
1
```

```
λ> fst (1,2,3)
```

```
... type error
```

Attention: `fst` is a function applied to **one** argument: the (two-element) tuple `(1,2)`.

A Simple Program (a reading exercise)

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`input`

`:: string`

`input`

A Simple Program (a reading exercise)

lines input

input :: string

lines input :: list of strings (lines)

A Simple Program (a reading exercise)

```
length (lines input)
```

```
input      :: string
```

```
lines input :: list of strings (lines)
```

```
length (lines input) :: number of lines
```

A Simple Program (a reading exercise)

```
lineCount input = length (lines input)
```

```
input           :: string
```

```
lines input     :: list of strings (lines)
```

```
length (lines input) :: number of lines
```

```
lineCount input :: function of one argument (input)
```

A Simple Program (a reading exercise)

```
interact lineCount
where lineCount input = length (lines input)
input      :: string
lines input :: list of strings (lines)
length (lines input) :: number of lines
lineCount input      :: function of one argument (input)
```

`interact` is function that “makes `lineCount` interact with the input”.

A Simple Program (a reading exercise)

```
interact lineCount
where lineCount input = show (length (lines input))
input                :: string
lines input          :: list of strings (lines)
length (lines input) :: number of lines
lineCount input      :: function of one argument (input)
```

`interact` is function that “makes `lineCount` `interact` with the input”.

`show` is function that `converts` “anything” to a string.

A Simple Program (a reading exercise)

```
main = interact lineCount
where lineCount input = show (length (lines input))

input           :: string
lines input     :: list of strings (lines)
length (lines input) :: number of lines
lineCount input :: function of one argument (input)
```

`interact` is function that “makes `lineCount` interact with the input”.

`show` is function that converts “anything” to a string.

`main` is the entry point of the program.

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1. The Basics
2. The Types
3. The Functions
4. The Real Functional Programming
5. The Fun

Types

In Haskell, **every** expression has a **type**.

The **type** of an expression is specified using **::**

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```
λ> :type True
```

```
True :: Bool
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```
λ> :type "Nightwish"
```

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```
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```

```
λ> :type "Nightwish"
```

```
"Nightwish" :: [Char]
```

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In Haskell, **every** expression has a **type**.

The **type** of an expression is specified using **::**

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```
True :: Bool
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```

```
"Nightwish" :: [Char]
```

```
λ> :t 2 + 3
```

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The **type** of an expression is specified using **::**

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```
True :: Bool
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```
"Nightwish" :: [Char]
```

```
λ> :t 2 + 3
```

```
2 + 3 :: Num a => a
```

Types

In Haskell, **every** expression has a **type**.

The **type** of an expression is specified using **::**

```
λ> :type True
```

```
True :: Bool
```

```
λ> :type "Nightwish"
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```
"Nightwish" :: [Char]
```

```
λ> :t 2 + 3
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```

└──────────┘
typeclass

Haskell's Types

Strong

- ▶ granular types (lots of details)
- ▶ no automatic coercion

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Static

- ▶ the type of anything is known at compile time

Haskell's Types

Strong

- ▶ granular types (lots of details)
- ▶ no automatic coercion

Static

- ▶ the type of **anything** is known at compile time

Inferred

- ▶ the type of **anything** is deduced automatically
 - ▶ almost anything

The Basic Types

Char	a Unicode character
Bool	True or False
Int	signed, 32- or 64-bit integer values, depending on the architecture
Integer	signed integers of unbounded size (more expensive than Int)
Double	floating-point numbers, typically 64 bits long, uses native floating-point representation
Float	narrower than Double, but much slower than Double, so its use is discouraged

Basic Composite Types: Lists and Tuples

```
λ> [1,2,3] :: [Int]
```

```
[1,2,3]
```

```
λ> (1,2,3) :: (Int,Int,Int)
```

```
(1,2,3)
```

Basic Composite Types: Lists and Tuples

```
λ> [1,2,3] :: [Int]
```

```
[1,2,3]
```

```
λ> (1,2,3) :: (Int,Int,Int)
```

```
(1,2,3)
```

```
λ> (True,"three") :: (Bool,String)
```

```
(True,"three")
```

A **tuple type** describes the **type** of **each component**.

Basic Composite Types: Lists and Tuples

```
λ> [1,2,3] :: [Int]
```

```
[1,2,3]
```

```
λ> (1,2,3) :: (Int,Int,Int)
```

```
(1,2,3)
```

```
λ> (True,"three") :: (Bool,String)
```

```
(True,"three")
```

A **tuple type** describes the **type** of **each component**.

[1,2] and [1,2,3] are of the **same type**

▶ [1,2] :: [Int] and [1,2,3] :: [Int]

(1,2) and (1,2,3) are of **different types**

▶ (1,2) :: (Int, Int) and (1,2,3) :: (Int, Int, Int)

No Functions Working on All Tuples

$(1,2)$ and $(1,2,3)$ are of different types

- ▶ $(1,2) :: (\text{Int}, \text{Int})$ and $(1,2,3) :: (\text{Int}, \text{Int}, \text{Int})$

No Functions Working on All Tuples

$(1,2)$ and $(1,2,3)$ are of different types

▶ $(1,2) :: (\text{Int}, \text{Int})$ and $(1,2,3) :: (\text{Int}, \text{Int}, \text{Int})$

Conclusion: it is **not** (directly) **possible** to define a function accepting tuples of **any length**.

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Function Types

```
λ> head [1,2,3]
```

```
1
```

```
λ> tail [1,2,3]
```

```
[2,3]
```

Function Types

```
λ> head [1,2,3]
```

```
1
```

```
λ> tail [1,2,3]
```

```
[2,3]
```

```
λ> :type head
```

Function Types

```
λ> head [1,2,3]
```

```
1
```

```
λ> tail [1,2,3]
```

```
[2,3]
```

```
λ> :type head
```

```
head :: [a] -> a
```

Function Types

```
λ> head [1,2,3]
```

```
1
```

```
λ> tail [1,2,3]
```

```
[2,3]
```

```
λ> :type head
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```
head :: [a] -> a
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```
λ> :type tail
```

Function Types

```
λ> head [1,2,3]
```

```
1
```

```
λ> tail [1,2,3]
```

```
[2,3]
```

```
λ> :type head
```

```
head :: [a] -> a
```

```
λ> :type tail
```

```
tail :: [a] -> [a]
```

Function Types: Polymorphism

`head :: [a] -> a`

Function Types: Polymorphism

`head :: [a] -> a`

`a` is a **type variable** : `a` can be of **any type**.

Function Types: Polymorphism

$$\text{head} :: [a] \rightarrow a$$

`a` is a **type variable** : `a` can be of **any type**.

`head` is a **function** taking a **list** of **any type** and returning an element of that **type**.

Function Types: Polymorphism

$$\text{head} :: [a] \rightarrow a$$

`a` is a **type variable** : `a` can be of **any type**.

`head` is a **function** taking a **list** of **any type** and returning an element of that **type**.

`head` is a **polymorphic function**.

Function Types: Polymorphism

$$\text{head} :: [a] \rightarrow a$$

`a` is a **type variable** : `a` can be of **any type**.

`head` is a **function** taking a **list** of **any type** and returning an element of that **type**.

`head` is a **polymorphic function**.

Types give a rather **detailed description** of what a **function** may do.

Function Types: Multiple Arguments

$$f \quad :: \quad a \rightarrow b \rightarrow c$$

Function Types: Multiple Arguments

$$f \quad :: \quad \underbrace{a \rightarrow b}_{\text{arguments}} \rightarrow \underbrace{c}_{\text{return value}}$$

Function Types: Multiple Arguments

$f :: \underbrace{a \rightarrow b}_{\text{arguments}} \rightarrow \underbrace{c}_{\text{return value}}$

$f \ x \ y :: c$

Function Types: Multiple Arguments

$$f \quad :: \quad \underbrace{a \rightarrow b}_{\text{arguments}} \rightarrow \underbrace{c}_{\text{return value}}$$
$$f \ x \ y \quad :: \quad c$$
$$f \ x \quad :: \quad b \rightarrow c$$

$f \ x$ is a function of **one argument**.

Function Types: Multiple Arguments

$$f \quad :: \quad \underbrace{a \rightarrow b}_{\text{arguments}} \rightarrow \underbrace{c}_{\text{return value}}$$
$$f \ x \ y \quad :: \quad c$$
$$f \ x \quad :: \quad b \rightarrow c$$

$f \ x$ is a function of **one argument**.

$$f \quad :: \quad a \rightarrow (b \rightarrow c)$$

f is a function of **one argument** **returning** a function of **one argument**.

Function Types: Multiple Arguments

$$f \quad :: \quad \underbrace{a \rightarrow b}_{\text{arguments}} \rightarrow \underbrace{c}_{\text{return value}}$$
$$f \ x \ y \quad :: \quad c$$
$$f \ x \quad :: \quad b \rightarrow c$$

$f \ x$ is a function of **one argument**.

$$f \quad :: \quad a \rightarrow (b \rightarrow c)$$

f is a function of **one argument** **returning** a function of **one argument**.

$f \ x$ is called **partially applying** f .

Lists: take and drop

```
λ> :t take
```

```
take :: Int -> [a] -> [a]
```

Lists: take and drop

```
λ> :t take
```

```
take :: Int -> [a] -> [a]
```

```
λ> take 3 [1..5]
```

Lists: take and drop

```
λ> :t take
```

```
take :: Int -> [a] -> [a]
```

```
λ> take 3 [1..5]
```

```
[1,2,3]
```

```
λ> :t drop
```

```
drop :: Int -> [a] -> [a]
```

```
λ> drop 3 [1..5]
```

Lists: take and drop

```
λ> :t take
```

```
take :: Int -> [a] -> [a]
```

```
λ> take 3 [1..5]
```

```
[1,2,3]
```

```
λ> :t drop
```

```
drop :: Int -> [a] -> [a]
```

```
λ> drop 3 [1..5]
```

```
[4,5]
```

Higher-order Functions

Higher-order functions take other functions as arguments.

$$\text{dup} :: a \rightarrow \underbrace{(a \rightarrow a \rightarrow b)}_{\text{that's one argument}} \rightarrow b$$
$$\text{dup } x \ f = f \ x \ x$$

Outline

1. The Basics
2. The Types
3. The Functions
4. The Real Functional Programming
5. The Fun

if statement

```
if condition
  then expression
  else expression
```

The newlines are not required.

```
λ> if True then putStrLn "yes" else putStrLn "no"
True
```


Recursion: the Factorial

Recursion: the Factorial

```
factorial :: Int -> Int
```

Recursion: the Factorial

```
factorial :: Int -> Int
factorial x = if x == 0
              then 1
              else x * factorial (x-1)
```

Recursion: the Fibonacci Series

Recursion: the Fibonacci Series

```
fibonacci :: Int -> Int
```

Recursion: the Fibonacci Series

```
fibonacci :: Int -> Int
fibonacci n = if n == 1
              then 1
              else if n == 2
                   then 1
                   else fibonacci (n-1)
                        + fibonacci (n-2)
```

Pattern Matching

How do I write `not` ? (for Booleans)

Pattern Matching

How do I write `not` ? (for Booleans)

```
not :: Bool -> Bool
```

```
not True = False
```

```
not False = True
```


Better Factorial

Better Factorial

```
factorial :: Int -> Int
factorial 0 = 1
factorial n = n * factorial (n-1)
```

Better Fibonacci Series

Better Fibonacci Series

```
fibonacci :: Int -> Int
fibonacci 1 = 1
fibonacci 2 = 1
fibonacci n = fibonacci (n-1)
              + fibonacci (n-2)
```

Pattern Guards

Pattern Guards

```
fibonacci :: Int -> Int
fibonacci n | n <= 2 = 1
fibonacci n | n > 2 = fibonacci (n-1)
                    + fibonacci (n-2)
```

The first equation will only be picked if $n \leq 2$.

The Catch-all Pattern

How to define `isZero`?

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How to define `isZero`?

```
isZero :: Int -> Bool
```

```
isZero 0 = True
```

```
isZero _ = False
```


The Catch-all Pattern

How to define `isZero`?

```
isZero :: Int -> Bool
```

```
isZero 0 = True
```

```
isZero _ = False
```

`_` matches **anything**, **without** giving it a **name**.

Pattern Matching on Lists and Tuples

```
λ> let list = [1,2,3]
```

```
λ> let [a,b,c] = list
```

```
λ> [c,a,b]
```

```
[3,1,2]
```

Pattern Matching on Lists and Tuples

```
λ> let list = [1,2,3]
```

```
λ> let [a,b,c] = list
```

```
λ> [c,a,b]
```

```
[3,1,2]
```

```
λ> let (one,_) = (1,2)
```

```
λ> one
```

```
1
```

Deconstructing Lists

```
λ> let (x:xs) = [1,2,3]
```

```
λ> (x,xs)
```

```
(1, [2,3])
```

Deconstructing Lists

```
λ> let (x:xs) = [1,2,3]
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```
λ> (x,xs)
```

```
(1, [2,3])
```

```
head :: [a] -> a
```

```
tail :: [a] -> [a]
```

Deconstructing Lists

```
λ> let (x:xs) = [1,2,3]
```

```
λ> (x,xs)
```

```
(1, [2,3])
```

```
head :: [a] -> a
```

```
head (x:_) = x
```

```
tail :: [a] -> [a]
```

Deconstructing Lists

```
λ> let (x:xs) = [1,2,3]
```

```
λ> (x,xs)
```

```
(1, [2,3])
```

```
head :: [a] -> a
```

```
head (x:_) = x
```

```
tail :: [a] -> [a]
```

```
tail (_:xs) = xs
```

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Anonymous Functions (Lambda Abstraction)

`(\ arguments -> expression)`

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$(\backslash \text{arguments} \rightarrow \text{expression})$

$(\backslash x y \rightarrow x + y)$

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`(\ x y -> x + y)`

`λ> let f = (\ x y -> x + y)`

Anonymous Functions (Lambda Abstraction)

`(\ arguments -> expression)`

`(\ x y -> x + y)`

```
λ> let f = (\ x y -> x + y)
```

```
λ> f 1 2
```

```
3
```

Anonymous Functions (Lambda Abstraction)

$(\backslash \text{arguments} \rightarrow \text{expression})$

$(\backslash x y \rightarrow x + y)$

$\lambda > \text{let } f = (\backslash x y \rightarrow x + y)$

$\lambda > f \ 1 \ 2$

3

Same thing as $f \ x \ y = x + y$

Sections

Partial application of operators.

$$(+)$$

```
 :: Int -> Int -> Int
```

Sections

Partial application of operators.

$(+)$:: Int -> Int -> Int

$(+ 2)$:: Int -> Int

Sections

Partial application of operators.

$$(+)$$
 :: Int -> Int -> Int
$$(+ 2)$$
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$$(+ 2) == (\ x \rightarrow x + 2)$$

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Note: sections preserve positions of the arguments:

$$(- 2) == (\ x -> x - 2)$$

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Partial application of operators.

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 :: Int -> Int -> Int
$$(+ 2)$$
 :: Int -> Int
$$(+ 2) == (\ x \rightarrow x + 2)$$

Note: sections preserve positions of the arguments:

$$(- 2) == (\ x \rightarrow x - 2)$$
$$(2 -) == (\ x \rightarrow 2 - x)$$

Folds

Fold = apply a **function** to every **element** of the list, accumulating a **result** on the way.

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```
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```

```
λ> foldl (+) 1 [1,2,3]
```

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foldl :: (b -> a -> b) -> b -> [a] -> b
```

```
λ> foldl (+) 1 [1,2,3]
```

```
[ 1 , 2 , 3 ]
```

```
1 +
```

Folds

Fold = apply a **function** to every **element** of the list, accumulating a **result** on the way.

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`[1 , 2 , 3]`
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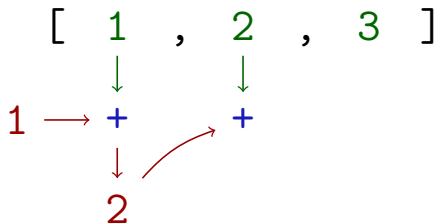
`[1 , 2 , 3]`
↓
`1 → +`
↓
`2`

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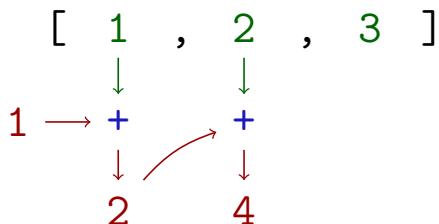


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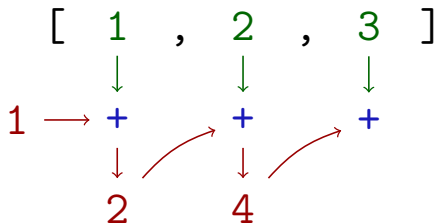


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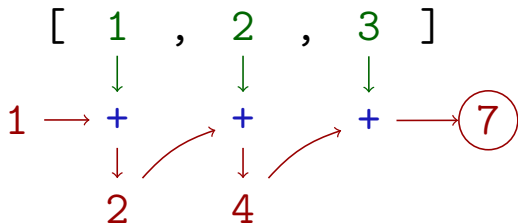


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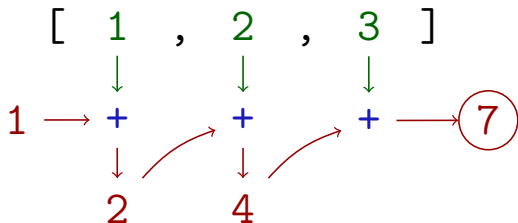


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`foldl :: (b -> a -> b) -> b -> [a] -> b`

`λ> foldl (+) 1 [1,2,3]`



`foldr` does the same thing from the **right** to the left.

The Rest of the Fun is Online

The code shown during [The Fun Session](#) is [online!](#)